

CS 598 WSI, LECTURE 5

- Narrowband vs. wideband channel
- OFDM: Motivation
- OFDM: Transmitter
- OFDM: Receiver.

NARROWBAND vs. WIDEBAND

Bandwidth

Symbol/s.

Wideband \Rightarrow

\uparrow bandwidth

\Downarrow

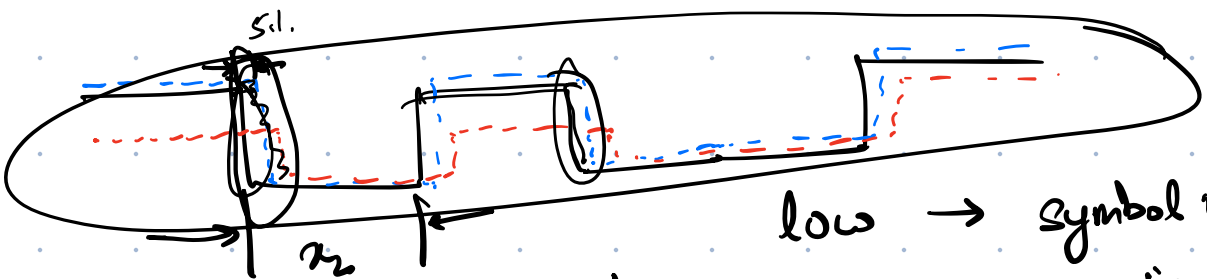
\uparrow data rate

Capacity = $\frac{BW \log(1+SNR)}{\text{bandwidth}}$

Inter-symbol Interference (ISI)

x_1, x_2, \dots, x_{100}

1ms 10 μ s \approx 1%



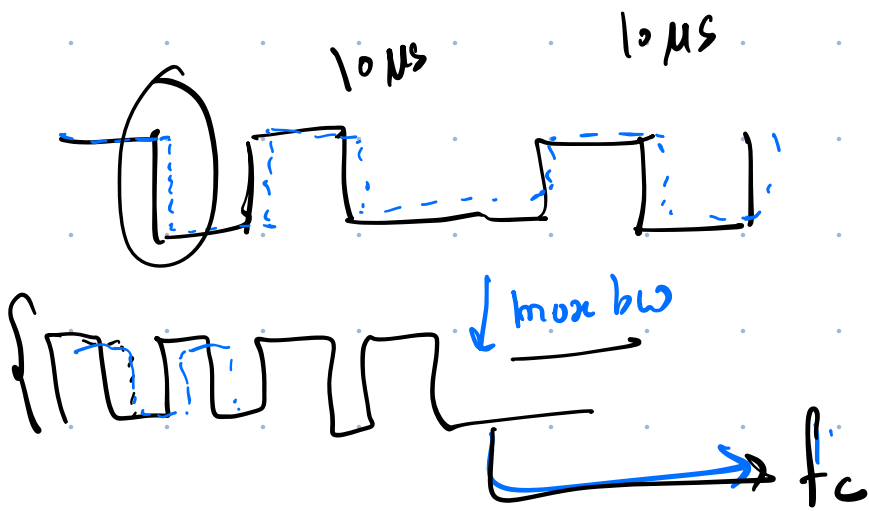
\hookrightarrow bandwidth

low \rightarrow symbol is longer in time

1000 \rightarrow 1ms

10000 \rightarrow 0.01ms

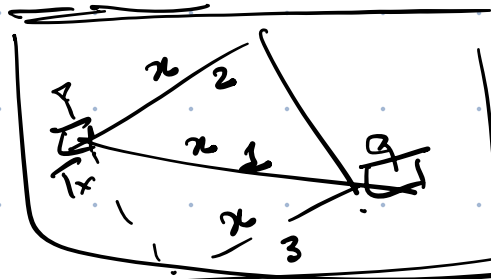
ISI
 For smaller the symbol \Rightarrow more the confusion due to ISI



CHANNEL

$$y = h x + n$$

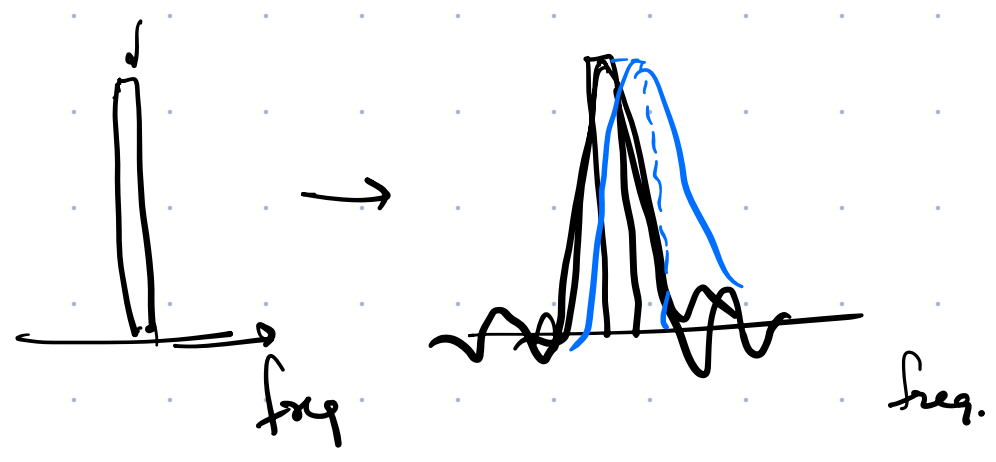
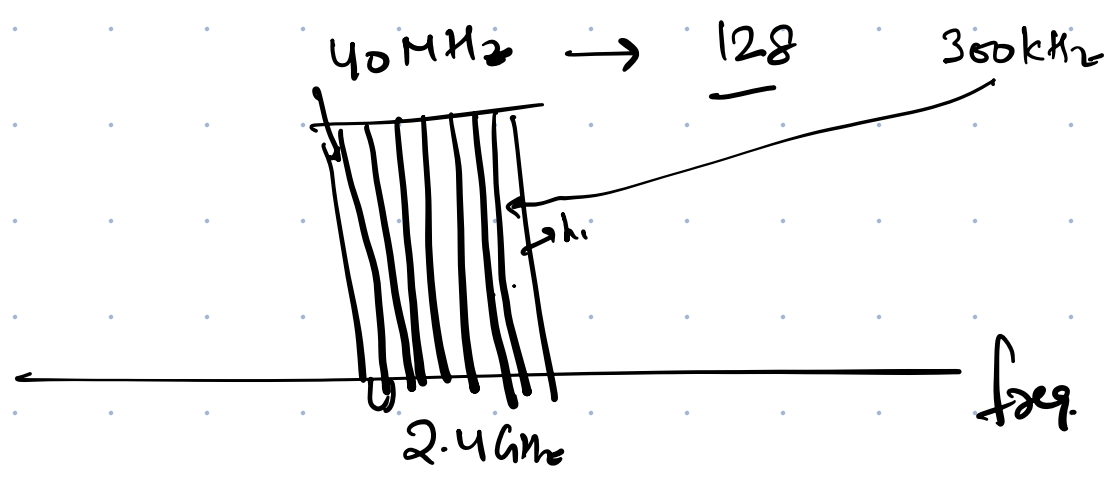
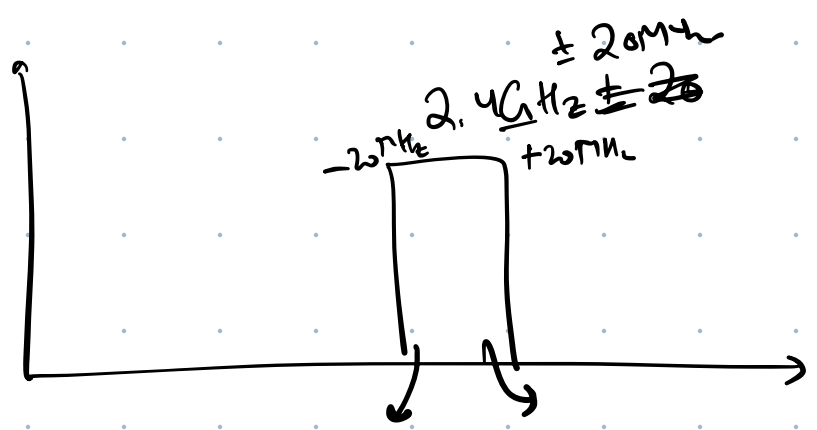
Labels: R_p (Receiver Power), T_x (Transmitter Power), noise, x (input signal)



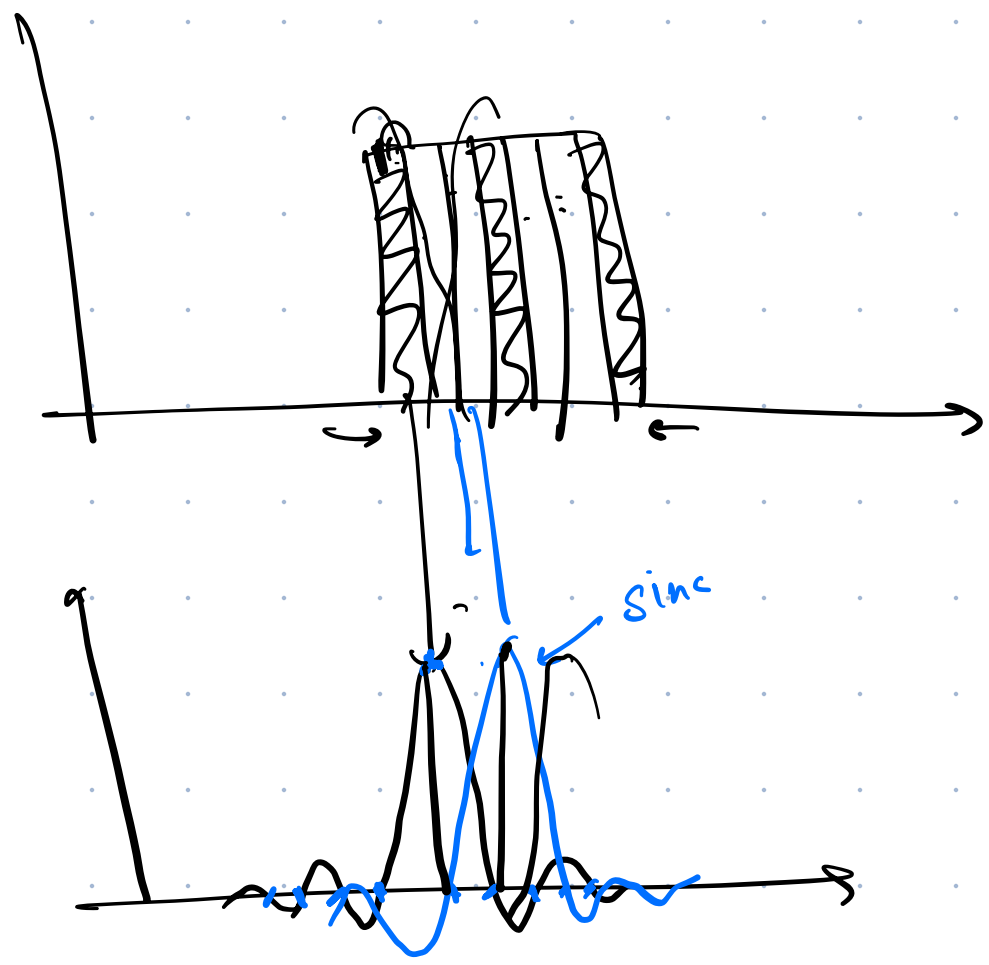
$$y(t) = h_1 x(t - \tau_1) + h_2 x(t - \tau_2) + h_3 x(t - \tau_3)$$

Labels: delay of path

Wideband channel \rightarrow occupies more spectrum / frequencies



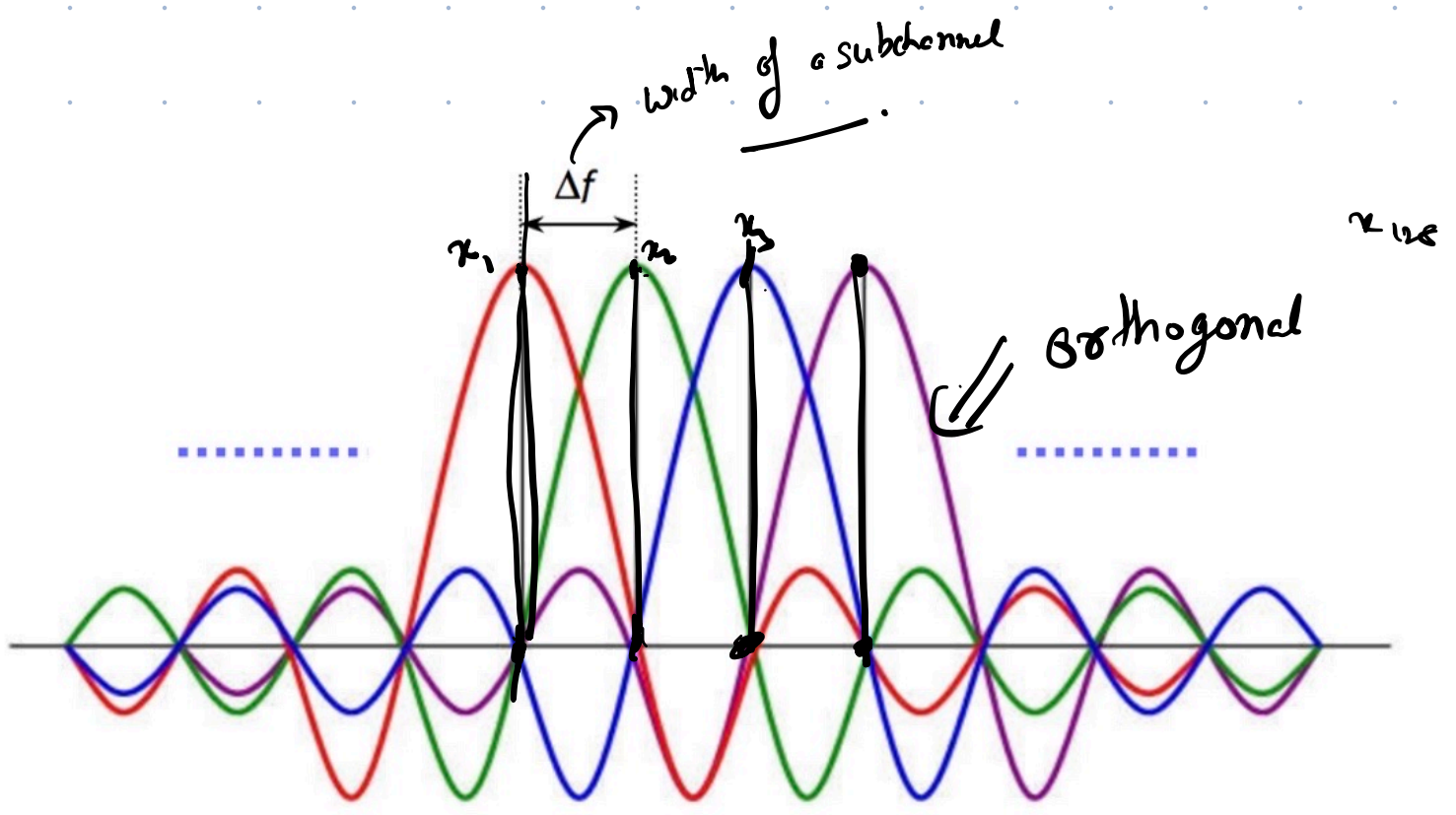
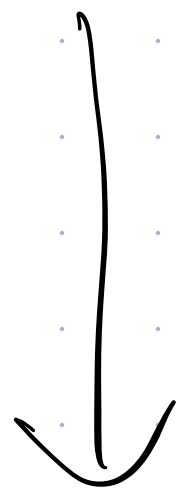
MULTIPLE NARROW BAND



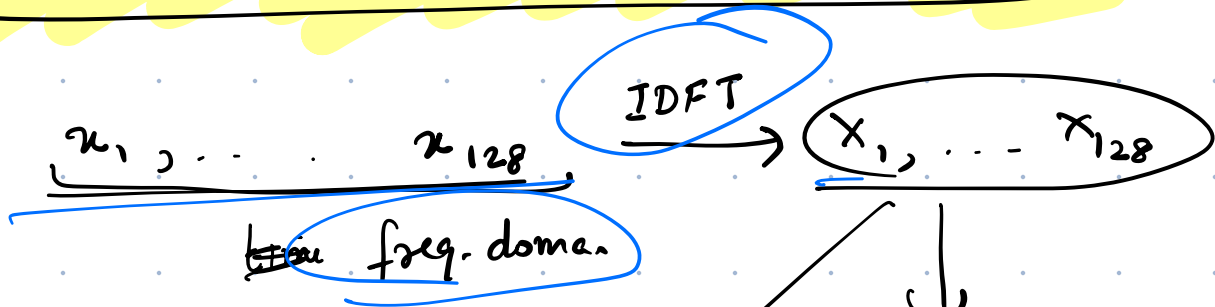
OFDM: MOTIVATION

DFT | Discrete Fourier Transform.

time domain \leftrightarrow frequency domain



OFDM: HOW DO YOU DO IT?



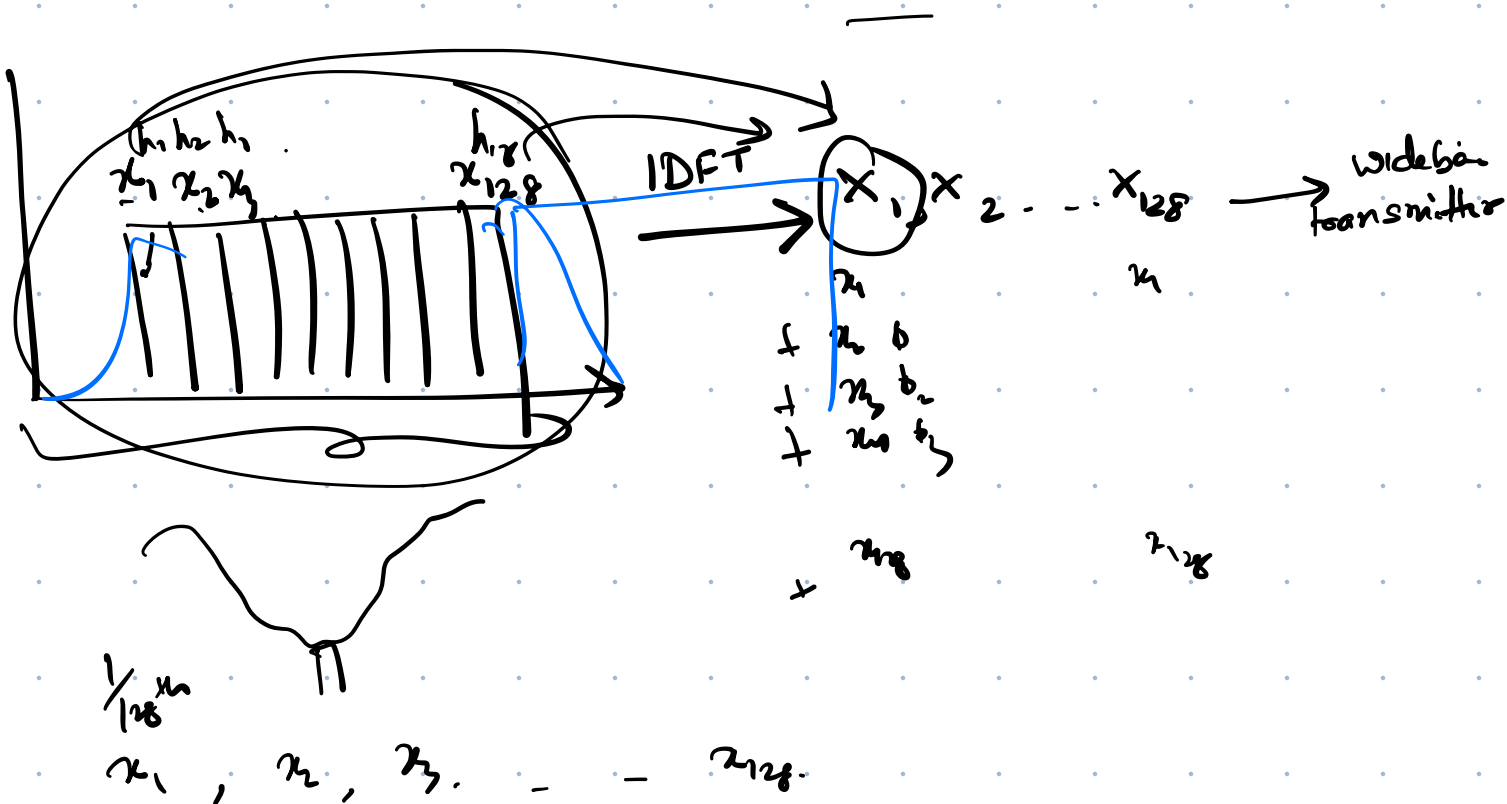
Wideband transmitter

X_1, X_2, \dots, X_{128}

$$X_f = \sum_{n=0}^{N-1} x_n e^{-j 2\pi f \frac{n}{N}}$$

\downarrow
 time

OFDM: Orthogonal frequency domain multiplexing.



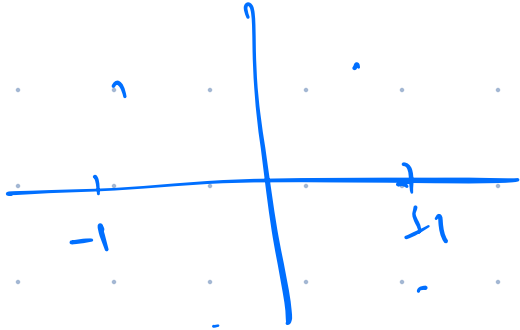


$$1 \text{ kHz} \rightarrow 1000 \text{ samples/s}$$



each symbol takes _{ms}

$$1 \text{ MHz} \rightarrow 10^6 \text{ samples/s}$$



$$8 \text{ MHz}, 128 \Rightarrow 600 \text{ kHz}$$

$$\frac{1}{600 \times 10^3 \text{ s}}$$

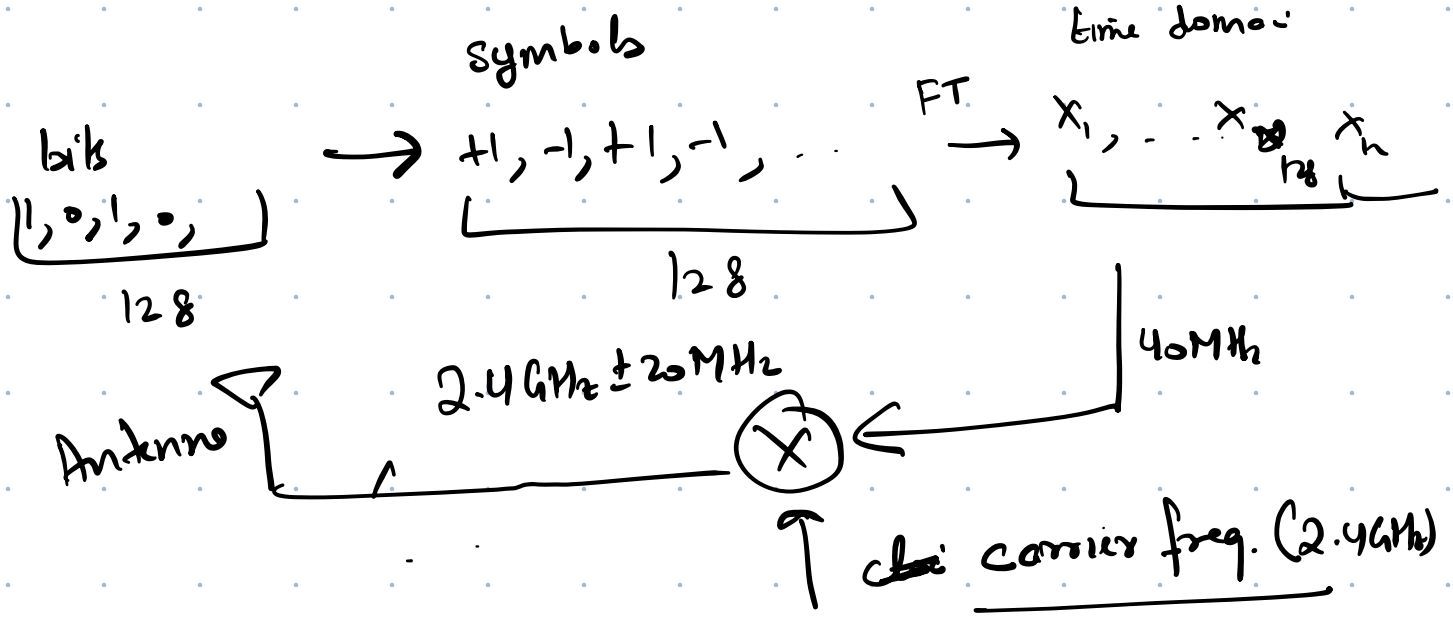
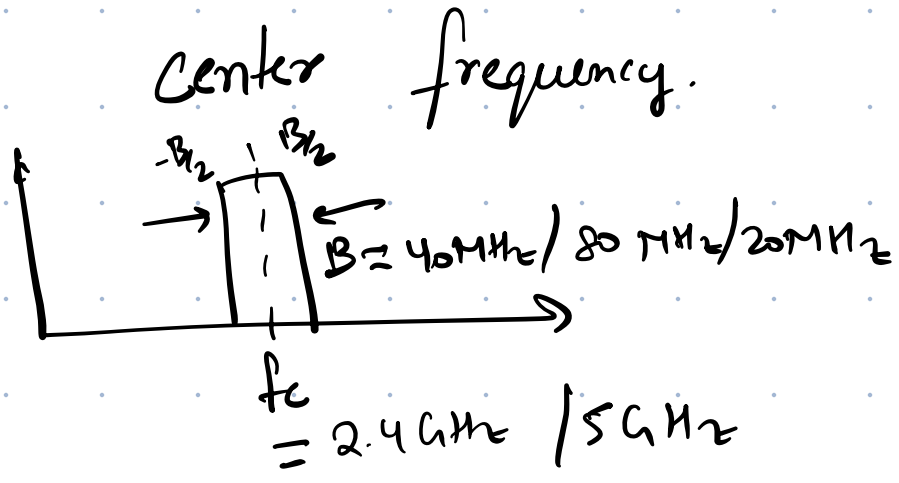
$$40 \text{ MHz}, 128 \Rightarrow \underline{\underline{300 \text{ kHz}}}$$

$$\frac{1}{300 \times 10^3 \text{ s}}$$

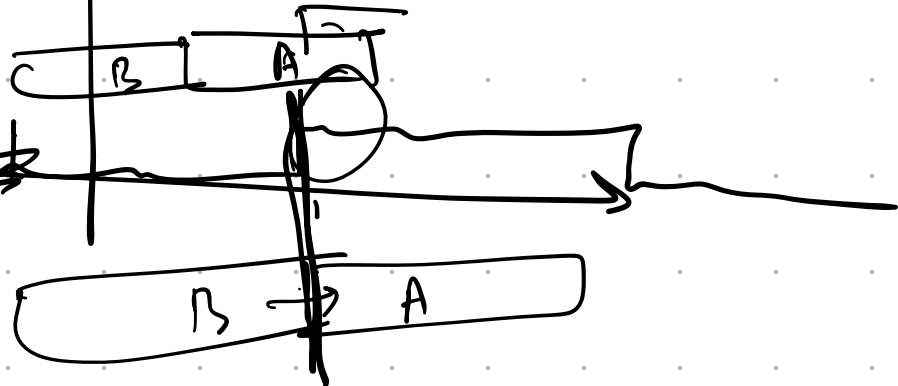
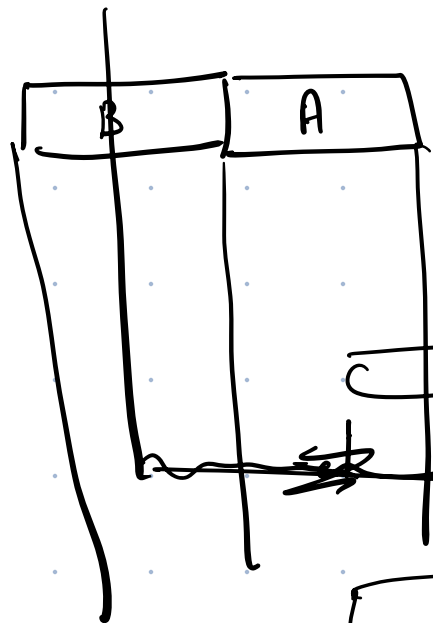
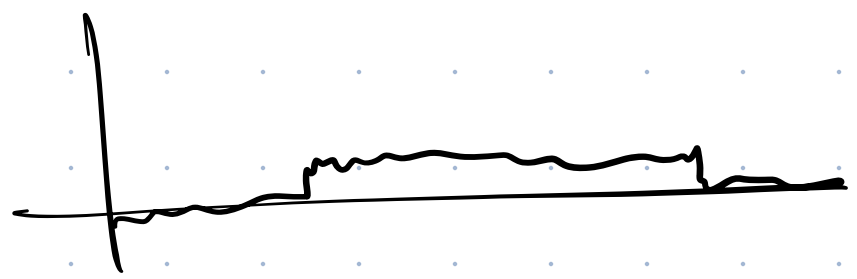
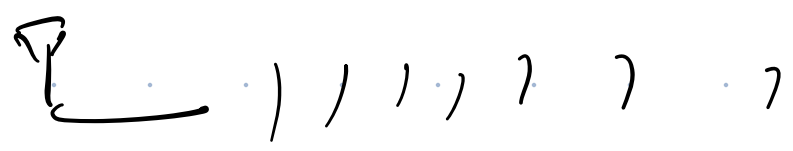
$$40 \text{ MHz}, 256 \Rightarrow 150 \text{ kHz}$$

$$\frac{1}{150 \times 10^3 \text{ s}}$$

OFDM: TRANSMITTER



OFDM: PACKET DETECTION



Sliding window packet detection.

